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On the Role of Theory and Evidence in Macroeconomics

Katarina Juselius
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Katarina Juselius
Department of Economics, University of Copenhagen
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Abstract

This paper, which is prepared for the Inagural Conference of the Institute for New Economic Thinking in King’s College, Cambridge, 8-11 April 2010, questions the preeminence of theory over empirics in economics and argues that empirical econometrics needs to be given a more important and independent role in economic analysis, not only to have some confidence in the soundness of our empirical inferences, but to uncover empirical regularities that can serve as a basis for new economic thinking.

1 Introduction

In 1991, the Scandinavian Journal of Economics organized a conference ‘New Approaches to Empirical Economics’ in which Lawrence Summers contributed the paper ‘The Scientific Illusion in Empirical Economics’ (Summers, 1991). He argued in the paper that empirical economics has exerted little influence on the development of economic theory and provided little new insight on economic mechanisms. As an illustration, he mentioned empirical analysis of representative agent models, which involves estimating a few deep parameters characterizing preferences and technology. He contrasted this analysis with sophisticated statistical techniques that impose minimal theoretical constraints on the data, as exemplified by a Vector AutoRegressive (VAR) model à la Sims. Summers argued that both approaches have been unable to explain the inherently richer and more complicated macroeconomic reality. He concluded that less formal examination of so-called stylized facts (correlations, mean growth rates, graphs) has resulted in more fruitful economic research.

Almost twenty years have passed since Summer’s critique and the INET conference seems like a good opportunity to revisit his main arguments. Has the marriage between theory and evidence improved? Has empirical economics become more enlightening?

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One of the key developments that can be seen as a response to Summer’s critique has been the so called Dynamic Stochastic General Equilibrium (DSGE) models of the macroeconomy. These models combine the assumptions of a representative agent and the "Rational Expectations Hypothesis" (REH) together with a dynamic stochastic structure à la Sims’ VAR. The added dynamics and stochasticity render the model more flexible than earlier representative agent models. Nonetheless, as it is practiced, one could say that the DSGE approach gives the primary role to the theory model and a subordinate role to the VAR. In this sense it embodies a preeminence of theory over empirics or what I call the 'theory-first' approach. The popularity of these models in graduate programs and among editors of top economics journals and researchers at central banks might suggest that economics as a science has finally converged to a state of unanimity both regarding theory and how to apply it to data.

This view was challenged when the crisis struck with a suddenness that took most economists, central bankers, and politicians by complete surprise. Obviously, standard models must have lacked important features as they failed to warn their users about the growing vulnerability of the macroeconomy to the crisis. As the crisis accelerated, the chorus of critical voices became a tsunami that washed over newspapers, blogs, etc. The debate on how to do economics was again fresh and alive. See for example discussions in Colander et al. (2009), Katlesky (2009), Lejonhufvud (2009), Krugman (2009), Cochrane (2009), Juselius (2009a, 2010a), Lawson (2009). Summers’ critique of the scientific value of empirical models in economics seems as relevant as it was 20 years ago.

In this paper, I question the preeminence of theory over empirics in economics. To address Summers’ critique, empirical econometrics needs to be given a more important and independent role in economic analysis, not only to have some confidence in the soundness of our empirical inferences, but to uncover empirical regularities that can serve as a basis for new economic thinking.

In the first part of the paper I contrast the theory-first approach to bridging economic theory and empirical evidence with what I call the 'data-first' approach. To fix ideas, I make use of the article ‘Taking a DSGE Model to the Data Meaningfully’ (Juselius and Franchi, 2007), which provides a detailed discussion of ‘A Method for Taking Models to the Data’ (Ireland, 2004a). Since the discussion can be seen as a critical attack on Ireland’s paper, I would like to stress that it was chosen because it was well documented, all results are reproducible, and it uses sophisticated econometrics.

I then argue that one important reason why the DSGE theory-first approach does not seem to have resolved Summers’ critique is that it does not properly account for the pronounced nonstationarity, such as unit root persistence and breaks, typical of economic data, either from a theoretical or econometric point of view. To have some confidence in the soundness of the inference being made, the number of stochastic trends has to be tested not just assumed, parameter constancy has to be checked, not just assumed, dynamics have to properly fit the data, etc. I demonstrate that these features can be modelled and tested with the (cointegrated) VAR model and argue that the nonstationarity of the data has strong implications for how to model expectations and for the ceteris paribus clause in economic models. This data-first
approach shows how economic theory can be confronted with the basic regularities in the data, thereby exposing any inconsistencies.

In the second part of the paper, I discuss how a statistically adequate VAR analysis often delivers additional (often theoretically puzzling) results. If these are taken seriously, they can generate new economic hypotheses that subsequently can be tested on new data. Thus, a VAR analysis based on full information maximum likelihood analysis of the data can be used both in a hypotheses testing and a hypotheses generating context. In the latter case the idea is to replace ‘simple stylized facts’ such as correlations, graphs, etc. with more sophisticated facts that better describe the nonstationary world in which individual decisions and market outcomes unfold. By doing so, it has the potential of providing a basis for new economic thinking.

2 Theory-First versus Data-First

The basic dilemma of empirical macro modelling is that the reality behind the available macroeconomic data is so much more rich and complex than the often narrowly analyzed problem being modeled by the theory. How to treat these ‘additional’ features of the data, which often go against the ceteris paribus assumptions of the economic model, has divided the profession into the proponents of the so called specific-to-general versus general-to-specific approach to empirical economics. To emphasize my subsequent arguments I shall here call them theory-first versus data-first. For a detailed methodological discussion of the two approaches, see for example Gilbert (1986), Hendry (1995, 2009), Juselius (2006), Pagan (1987) and Spanos (1995, 2006, 2009).

The former, more conventional, approach starts from a mathematical formulation of a theoretical model and then expands the model by adding stochastic components. The aim is to estimate the parameters of a ‘stylized’ economic model, while ignoring the wider circumstances under which the data were generated. These factors are then dumped into the residual term, causing its variance to be large. This practice has important implications for the power of empirical testing, often leading to a low ability to reject a theory model even when it provides a poor description of the basic regularities in the data. As a result, competing theory models are often not rejected despite being tested against the same data. Furthermore, the statistical inference in such models is usually based on a number of untested and empirically questionable assumptions so that the ‘significance’ of estimated parameters may lack scientific meaning.

This approach is strongly influenced by the legacy of the pre-eminence of theory, which presumes that the basic economic mechanisms can be pre-specified, i.e., we know which of the variables are exogenous, which do the adjusting when the system has been pushed out of steady-state, how various interventions have affected the system, etc. Econometrics in this case play the subordinate role of ‘quantifying’ theoretically meaningful parameters assumed to be empirically relevant on a priori grounds. This approach can only be defended if the probabilistic assumptions comprising the underlying statistical model are satisfied vis-à-vis the data in question (Spanos, 2009). If not, it produces empirically irrelevant and possibly misleading
results.

The data-first approach starts from an explicit stochastic formulation of all data (selected on the basis of the theory model in question) and then reduces the general statistical model by simplification testing. It answers the economic questions of interest by embedding the economic model within the statistical model and uses strict statistical principles as a criterion for a good empirical model. In this case, the statistical model ties economic theory to the data when it nests both the data-generating process and the theoretical model, so that the parameters of the theoretical model can be derived from the parameters of the statistical model (Hoover et al., 2008).

It recognizes from the outset the weak link between the theory model and the observed reality. For instance, few, if any, theory models fully allow for basic characteristics of macroeconomic data such as path dependence, unit-root nonstationarity, structural breaks, shifts in equilibrium means, and location shifts in general growth rates. Such empirical features of economic data are generally at odds with the prevailing theory-first paradigm, which assumes a few constant structural parameters describing technology and preferences, REH and some ad hoc dynamics. In contrast, the data-first methodology works by allowing the empirical regularities in data to speak as freely as possible about underlying theoretical relationships, thereby allowing us to discriminate between empirically relevant and irrelevant theories, but also to discover new evidence for which prior hypotheses have not yet been formulated. All this will be discussed in the next sections using Ireland (2004a) as an illustrative case study.

3 Ireland’s DSGE model: a first check

The hypothesis that aggregate technology shocks alone drive business cycle fluctuations, is a key feature of the real business cycle (RBC) model discussed in Ireland (2004a). More specifically, the model assumes a utility maximizing representative agent, who chooses between consumption and total hours worked in an economy subject to a constant returns to scale technology described by the Cobb Douglas production function. The latter is defined for capital and labor subject to labor-augmented technological progress, which is assumed to have grown with a constant rate over the examined period 1948-2002. Capital and total factor productivity are assumed to be unobserved and generated from cumulated identical shocks. The model describes a closed economy without a government sector.

To take the highly nonlinear RBC model to the data, Ireland log-linearizes around theoretical steady-state values making use of the following basic assumptions: (i) total factor productivity follows a first order stationary autoregressive model and (ii) the growth rate of labor-augmenting technological progress is constant over time. The implications of these assumptions are that (i) trend-adjusted output, consumption, investment, and capital are stationary around their steady-state values, (ii) the rate of labor augmenting technological progress is constant and results in identical linear trends in output, consumption, investment and capital, and (iii) technology shocks are pushing both total factor productivity (TFP) and capital and define the main driving force. The model’s three equations (output, consumption, and labor) are made ‘more flexible’ by adding a VAR(1) process to them.
Most of its parameters are estimated using a Kalman filter nonlinear optimization routine that can handle the singularity of the model\(^1\). The exceptions being the parameters for depreciation rate and the discount rate, which are calibrated. The estimated structural parameters are constrained to satisfy the restrictions implied by theory.

The reported estimates are claimed to be maximum likelihood (ML) estimates. But ML requires that the assumptions underlying the model are correct. Thus, they have to be checked not just assumed. In this context it is useful to draw a distinction between substantive and statistical assumptions (Spanos, 2009) as their respective validity has different implications for inference. The substantive assumptions pertain to the centuries old issue of the realism of economic theories, whereas the statistical assumptions pertain to the reliability of the statistical inference. As the Ireland paper did not report tests of these assumptions, Juselius and Franchi (2007) first replicated all results reported in Ireland’s paper and then performed a detailed check of the statistical as well as of some of the substantive assumptions.

Parameter constancy is one of the substantive assumptions: If parameters are structural they ought to remain constant despite changes in policy regimes. Over the sample period, the US economy experienced a major policy regime shift around 1979. In a footnote, Ireland mentions that parameter constancy before and after this date has been tested and rejected. Nonetheless he disregarded this evidence, because parameter estimates were ‘quite similar’ before and after that date.

The stationarity assumption needed for the log-linearization around the constant steady-states can be assessed based on estimates of the characteristic roots of the model, of which the largest were 0.9987, 0.94 and 0.88.\(^2\) A root of 0.9987 is admittedly less than one, but in practice indistinguishable from a unit root. Even a root of 0.94 is pretty close to unity suggesting an additional source of pronounced persistence in the data.

One consequence of the assumptions of identical deterministic growth rates for output, consumption and capital, when the actual rates differed markedly, and stationarity, when there are near unit roots in the data, can be inferred from Figure 1\(^3\). The deviations from the assumed steady-state values are very persistent and systematically either positive or negative. Except for hours worked, they never cross the zero line over a period of fifty years!

The statistical misspecification tests of Ireland’s model showed that the null of residual normality, no autocorrelation, and no ARCH were rejected for essentially all variables. Furthermore, the cross correlogram showed significant correlations between the errors which are assumed independent. Thus, a first set of diagnostic tests revealed a clear violation of the assumed distributional assumptions. Hence, the assumed probability model is not correctly specified; the reported statistical inference is not Maximum Likelihood and the p-values calculated from standard normal distributions (\(t\), \(F\), and \(\chi^2\)) may be completely unreliable. In particular,

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\(^1\)Because the technology shock is the only source of randomness in the model, the model is stochastically singular.

\(^2\)The simulation in Johansen (2006) shows that with a root of 0.9987, at least 5000 observations are needed for getting close to the correct size of a test on the steady-state value.

\(^3\)These were not reported in Ireland, but derived from his model.
the assumption that data are stationary, when in fact they are very close to being nonstationary, is likely to make all inference on steady state values meaningless (see Johansen, 2006).

There is, however, an easy solution to the problem of unit roots in the data and its effect on inference. By transforming the data into stationary components using differencing and cointegration (see for example, Engle and Granger 1987; Hendry 1987, 2009; Johansen 1988, 1995; Juselius, 2006) standard inference would apply again. This is also the preferred solution in Ireland (2004b). Juselius and Franchi (2007), therefore, examine whether the RBC hypothesis is, nevertheless, a good description of US business cycles. This is done by recasting the basic hypotheses in the Ireland model as statistical tests on a well-specified Cointegrated VAR (CVAR) model.\footnote{Gross capital formation is used as a measure of capital instead of the Ireland variable which was generated to fit the RBC hypothesis.}

4 The RBC hypothesis: A CVAR check

4.1 A theory consistent CVAR scenario

To test the basic RBC assumptions underlying Ireland’s DSGE model formulation, we need to formulate all basic (substantive and statistical) assumptions as testable hypotheses on the VAR model. Such a theory-consistent VAR scenario can be seen as a bridge between the theory model and the VAR and is a summary of necessary conditions on the data for the model to be empirically relevant.
One of the roots (associated with total factor productivity) was very close to unity and was approximated with a unit root, i.e. we assume that total factor productivity, $a_t$, is a unit root stochastic process instead of an AR(1) with a near unit root:

$$a_t = a_{t-1} + \varepsilon_t = \sum_{i=1}^{t} \varepsilon_i + a_0,$$

where $\varepsilon_t$ is a permanent TFP shock. The cumulation of these shocks, $\sum_{i=1}^{t} \varepsilon_i$, is called a (first order) stochastic trend and describes the development of total factor productivity over time. A variable containing a first order stochastic trend is called integrated of order one, in short I(1). The difference between a first order stochastic and a deterministic linear trend is that the permanent increments of a stochastic trend change randomly, whereas those of a deterministic trend are constant over time.

When two variables share the same cumulated permanent shocks we say that the two variables are cointegrated. For example, if capital and income share the same TFP stochastic trend (1) it implies that they have followed the same long-run stochastic growth path and are therefore likely to be causally associated. In a growing economy, many variables would likely also share a linear deterministic trend, but such trends can easily be spurious as the source of the linear increment is generally not identified. Therefore, finding significant cointegration is a much more demanding and relevant measure of long-run association than finding a significant regression relationship. For an expository introduction to integration and cointegration see Hendry and Juselius (1999, 2000).

Furthermore, the advantage of classifying data according to their order of integration, I(0), I(1) and I(2)$^5$ is that it allows us to classify variables and relations according to their "persistency profiles", i.e. we can discriminate between relations which exhibit pronounced persistence and relations which do not. For example, the strong persistence visible in the graphs of the steady-state errors in Figure 1 suggests that the long-run path of Ireland’s data is not adequately described by a deterministic trend and that the steady-state errors contain a stochastic trend which needs to be eliminated by cointegration.

Assuming one stochastic trend and three cointegration relations, a theory consistent CVAR scenario for Ireland’s model is given by:

$$
\begin{bmatrix}
  y_t \\
  c_t \\
  h_t \\
  k_t
\end{bmatrix} = 
\begin{bmatrix}
  d_1 \\
  d_1 \\
  d_1 \\
  d_1
\end{bmatrix} 
\begin{bmatrix}
  a_t \\
  [t] \\
  [t] \\
  [t]
\end{bmatrix} +
\begin{bmatrix}
  b_1 \\
  b_1 \\
  b_1 \\
  b_1
\end{bmatrix} 
\begin{bmatrix}
  v_{1,t} \\
  v_{2,t} \\
  v_{3,t} \\
  v_{4,t}
\end{bmatrix}
$$

where, $y_t$ is the log of output, $c_t$ is the log of consumption, $h_t$ is the log of hours worked, $k_t$ is the log of capital, $a_t = \sum_{i=1}^{t} \varepsilon_i$ is the sum of total factor productivity shocks and $\varepsilon_t$ is a stationary MA process. It implies (i) a non-stationary Cobb-Douglas production function, $\{y_t - \theta k_t - (1-\theta)h_t\} \sim I(1)$, (ii) a stationary

$^5$Transitory shocks which do not cumulate are called I(0), permanent shocks which cumulate once are called I(1), and permanent shocks that cumulate twice are called I(2).
consumption/income ratio, \( c_t - y_t \sim I(0) \), (iii) a stationary capital/income ratio, \( k_t - y_t \sim I(0) \), and (iv) that hours worked is stationary, \( h_t \sim I(0) \). Thus, under scenario (2) the three cointegration relations should correspond to relations in (ii)-(iv)\(^6\).

According to Ireland’s model, shocks to technical progress should explain the development over time in TFP and capital, and output, consumption and labor would be pulling (i.e. endogenous). This can be formulated in the following equilibrium error correcting model:

\[
\begin{bmatrix}
\Delta y_t \\
\Delta c_t \\
\Delta h_t \\
\Delta k_t
\end{bmatrix} =
\begin{bmatrix}
\alpha_{11} & \alpha_{21} & \alpha_{31} \\
\alpha_{12} & \alpha_{22} & \alpha_{32} \\
\alpha_{13} & \alpha_{23} & \alpha_{33} \\
\alpha_{14} & \alpha_{24} & \alpha_{34}
\end{bmatrix}
\begin{bmatrix}
(c - y - \mu_{01})t^{-1} \\
(k - y - \mu_{02})t^{-1} \\
(h - \mu_{03})t^{-1}
\end{bmatrix} +
\begin{bmatrix}
b_1 \\
b_1 \\
0 \\
b_1
\end{bmatrix} +
\begin{bmatrix}
\varepsilon_{1,t} \\
\varepsilon_{2,t} \\
\varepsilon_{3,t} \\
\varepsilon_{4,t}
\end{bmatrix}
\] (3)

The scenarios (2) and (3) comprise a set of necessary conditions that need to be supported by the data for the Ireland RBC model to pass a first test of empirical relevance.

### 4.2 A CVAR reality check of Ireland’s model

An unrestricted VAR(2) model in levels was first estimated and tested for misspecification, and then revised accordingly. The null of constant parameters for the periods 1960:1-1979:4 and 1981:2-2002:1 was, however, strongly rejected; the assumption that the structural parameters are constant over time did not seem tenable with the information in the data. The VAR analysis was, therefore, done separately for the two periods and produced the following general results: (i) The first period was fairly well described by the estimated model, but the second period less so\(^7\); (ii) in both periods there seemed to be at least two stochastic trends (rather than one), one of which was associated with permanent shocks to consumption and the other to labor; (iii) a trend-stationary Cobb-Douglas production function with plausible coefficients seemed to work well in the first, but not in the second period; (iv) hours worked was found to be nonstationary against the stationarity assumption in Ireland’s model.

Altogether, the results suggested that total factor productivity and technological progress might have been well approximated by a linear trend in the first period but not in the second, and that it was demand shocks rather than shocks to TFP that have triggered off US business cycles. Thus, the information in the data seemed more consistent with a Keynesian than a RBC explanation of US business cycles. When this is said, the CVAR results should only be considered tentative as a better model specification is clearly needed. This is particularly so for the second period where the results were based on an econometrically unsatisfactory model.

Thus, the conclusion reached in Ireland’s paper (that the real business cycle theory model is able to explain the long business cycles in the US post war period)\(^8\)

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\(^6\)A similar transformation of the theoretical model into growth rates and cointegration is suggested in Ireland (2004b).

\(^7\)The second period contained a lot more persistence, and as will be illustrated below it is questionable whether there is any cointegration.
was not based on correct statistical inference and the conclusion was reversed when based on a well-specified CVAR model. In spite of the sophisticated dynamic and stochastic specification, Ireland’s DSGE model seemed to lack important features needed to properly account for the complexity of the economic reality: The basic predictions from Ireland’s DSGE model fell outside the confidence bands of the empirical reality.

4.3 Pulling sophisticated empirical facts out of data

Summers (1991) concluded his critique by claiming that a less formal examination of empirical facts has generally resulted in more fruitful economic research. While possibly useful, such stylized facts are nevertheless too coarse and can even be misleading when data are nonstationary because simple correlation coefficients and mean growth rates are only well defined for stationary, but not nonstationary, data (Yule, 1926).

The unrestricted VAR model, properly specified and tested, can be seen as a convenient summary of the covariances of the data (Hendry and Mizon 1993; Juselius 2006, Chapter 3) and, therefore, represents the reality we would like our theoretical model to describe. But, because the VAR is heavily overparametrized, it is not very informative as such. Its usefulness is in providing us with a framework within which we can reduce the number of parameters until further restrictions change the value of the likelihood function significantly. If correctly done, the final parsimonious VAR model would describe regularities in the data without suppressing any relevant information and, therefore, would provide a set of ‘statistical regularities’ that the theoretical model should explain in order to be empirically relevant.

In particular, by combining differenced and cointegrated data, the CVAR model offers a natural way of analyzing economic data as short-run variations around moving long-run equilibria. Longer run forces are themselves divided into the forces that move the equilibria (pushing forces, which give rise to stochastic trends) and forces that correct deviations from equilibrium (pulling forces, which give rise cointegrating relations). Interpreted in this way, the CVAR has a good chance of nesting a multivariate, path-dependent data-generating process and relevant dynamic macroeconomic theories. One could say that the CVAR model gives the data a rich context in which they are allowed to speak freely (Hoover et al., 2008). See also Framroze-Møller (2008) for a detailed exposition of how to translate basic concepts of macroeconomic models into testable concepts of the CVAR model.

The CVAR analysis of Ireland’s DSGE model illustrates this latter point: When data were allowed to speak freely, they speak about a number of empirical regularities that had been silenced by prior restrictions: the number of stochastic trends were two or three in the data, whereas one in Ireland’s model; the two driving forces originated from shocks to consumption and labor in the data, whereas from TFP and capital in Ireland’s model; the lag order of the VAR was two in the data, whereas one in Ireland’s model; the variables were trend nonstationary in the data, whereas trend-stationary in Ireland’s model; there was strong evidence of structural breaks in the data, whereas a constant DSGE structure was assumed in Ireland’s model.

An advantage of analyzing the Ireland data separately for the period before and
after 1980 was that it allowed us to compare similarities and differences between
the two periods and, therefore, get a first idea of which economic mechanisms had
changed and why. In particular, we were able to demonstrate that income, consump-
tion, labor, and capital did a reasonable job in ‘explaining’ business cycle movements
in the first period (though with a Keynesian flavor), but a much less satisfactory
one in the more recent period indicating that some important information is missing
in the theoretical set-up. Section 6 will argue that it is the globalization of
financial markets that have influenced US savings and investment decisions and this
information is missing in the present set-up.

5 Economic modelling and nonstationary data

The lack of empirical support may not come as a big surprise to economists, who
would argue that their models are not meant to be close approximations to the
economic reality. Many would argue that by adding new features to these models
they will gradually improve\(^8\). I would like to challenge this view and argue that the
strong evidence of nonstationarity in data points to a more fundamental problem
with many economic models that are intrinsically developed for a stationary world
despite containing some added-on persistence and dynamics. As will be discussed
below, nonstationarity has strong implications for important aspects of economic
models, such as the role of expectations, the relevance of risk and uncertainty, and
the empirical validity of the \textit{ceteris paribus} assumption.

5.1 The Role of Expectations in a Nonstationary World

The strong evidence of (near) unit roots and (structural) breaks in economic vari-
ables and relations suggest that economic behavior is often unpredictable. In such
a nonstationary world Clement and Hendry (1999, 2008) show that forecasts from
constant-parameter theory models, assumed to be correct from the outset, are likely
to perform poorly. Since rational expectations models imagine economic agents who
are able to recursively foresee future outcomes with known probabilities, they are
inconsistent with the prevalence of structural breaks in the data (Hendry and Mi-
zon, 2009). It may, therefore, not be surprising that these models often have a hard
time describing macroeconomic data. The strong prevalence of nonstationarity in
economic time series, in itself, is evidence of the fact that we do not know in which
direction the future is moving. To act as if we do would indeed be highly irrational.
In the words of Keynes (1937):

"By ‘uncertain’ knowledge, let me explain, I do not mean merely to distinguish what
is known for certain from what is only probable. The game of roulette is not subject, in
this sense, to uncertainty...The sense in which I am using the term is that in which the
prospect of a European war is uncertain, or the price of copper and the rate of interest
twenty years hence...About these matters there is no scientific basis on which to form any
calculable probability whatever. We simply do not know."

\(^8\)To cite an anonymous discussant to Spanos (2009): “I don’t think DSGE modelers don’t
care about the empirical support of their theories; they just have a different metric to assess the
usefulness of their theories. If the standard metric rejects the model, just choose a different metric.”
But, if rational expectations have to go, what should replace them? Frydman and Goldberg (2007, 2008) provide an alternative approach dubbed ‘Imperfect Knowledge Economics’ (IKE), which recognizes that the process driving outcomes in modern economies changes at times and in ways that no one can specify ahead of time up to a random error. Such change arises in part because individuals’s forecasting strategies, which play an important role in driving market outcomes, changes in ways that they themselves, let alone an economist, cannot fully prespecify. Once one recognizes the importance of imperfect knowledge, assuming constant ‘structural’ parameters, as the vast majority of economists do, makes little sense.

IKE holds out the possibility that, although change in modern economies does not unfold mechanically, it may exhibit qualitative regularities that can be modeled both theoretically and empirically. Because IKE models impose qualitative restrictions on change, it generates qualitative implications, which, though testable, are looser than those derived under REH. Johansen et al. (2010), Juselius (2010b), and Frydman et al. (2008) find that the implications of REH-based models of nominal and real exchange rates are strongly rejected in favor of IKE-based models.

One of the key implications of Frydman and Goldberg’s (2007, 2008) IKE model of asset markets is that imperfect knowledge can lead to greater persistence in asset price fluctuations than what is implied by REH-based models. This enables the model to account for the long swings in asset prices away from and toward benchmark levels that often characterize asset markets.

5.2 The Ceteris Paribus Assumption and Nonstationarity

It is a common practice to simplify a theory model by using the *ceteris paribus* assumption “everything else unchanged”. However, the empirical relevance of the *ceteris paribus* assumption in a theory model is likely to be strongly affected by the order of integration of the *ceteris paribus* variables. If they are stationary, the conclusions are more likely to remain robust than if they are nonstationary. This is because a nonstationary *ceteris paribus* variable if included in the empirical model is likely to influence the cointegration results and, therefore, the conclusions of the model’s steady-state behavior. Since no variables can be kept artificially fixed in the real economy, the empirical problem needs to be addressed in the context of “everything else changing” and the impact of the *ceteris paribus* variables needs to be brought into the analysis by conditioning.

Consider, for example, the empirical CVAR analysis of Ireland’s RBC model discussed in Section 4.2. Using Ireland’s data, we found that the first period up to 1979 was reasonably well described by two pulling and two pushing forces, though with a Keynesian rather than a RBC explanation of US business cycles. For the more recent period the chosen information set was not sufficient: there was only weak evidence of cointegration, suggesting that some important determinants are missing. This can be illustrated with the graphs of the first two cointegration relations (the first one describing deviations from a homogeneous Cobb-Douglas relation, the other from consumption - income ratio. There is a striking difference between the two periods: in the first period, deviations from fundamental long-run values are reasonably modest, in the second, these are characterized by long and persistent
Figure 2: The Cobb-Douglas function and the income-consumption ratio relation estimated over the two regimes.

Because a major difference between the two periods is the increasing globalization of financial markets, a first hypothesis that springs to mind is an increasing importance of prolonged swings in these markets. This would be consistent with the IKE theory discussed above as well as with the notion of reflexivity in Soros (1987, 1998, 2001, 2008). The latter would suggest that such pronounced movements away from long-run benchmark values would have a strong impact on the aggregate behavior in the real economy and vice versa.

However, if the information set is increased by new variables, such as financial and housing wealth, that are likely to reflect the booms and busts of global financial markets, previous empirical conclusions might not remain unchanged. For example, the extended model may show that it is empirical shocks to financial or housing wealth that are pushing the system and that consumption and the rest of the variables have been adjusting. Therefore, equating a residual with an autonomous shock, as Ireland and many others do, can be misleading unless the model contains all relevant variables.\footnote{This points to the importance of not just assuming that the model contains all basic relevant variables but also to check whether this is the case, for example by using automatic search procedures such as Autometrics (Hendry and Krolzig, 2005).}

Such concerns are, however, easily met as it is straightforward to increase the information set, building on previously obtained results (as the cointegration property is invariant to changes in the information set) thereby learning systematically how sensitive previous conclusions are to the \textit{ceteris paribus} clause. Thus, the CVAR story is not claimed to be ‘structural’ in the usual sense, albeit it often has a lot of empirical content. This is contrary to Ireland’s DSGE analysis which tells a ‘structural’ story, but with little empirical content.
6 ‘Sherlock Holmes’ econometrics

More than a quarter of a century ago, when Søren Johansen and I started working on the CVAR approach, I was taken by the beauty of this model, its rich structures and its potential for addressing highly relevant questions within a stringent statistical framework. What I did not expect was that the data consistently refused to tell the stories they were supposed to. After many frustrating attempts, it seemed that I had the choice of either forcing data to tell a theoretically acceptable story or approaching the complex reality without the guide of a reliable theory. I chose the latter and started using the Cointegrated VAR model in the spirit of Sherlock Holmes, an experience that best can be described as a long series of why’s.

Though economic puzzles are probably harder to solve than crimes, I believe it is in the Sherlock Holmesian spirit that a well structured empirical CVAR analysis can inspire new economic thinking. It is based on two important principles: (1) data are allowed to speak as freely as possible against a background of not just one but several theories, (2) falsification is considered more important than verification and results that go against conventional wisdom are considered more interesting than confirmatory results.\(^\text{10}\)

It has a Marshallian rather than a Walrasian flavour expressed by Kevin Hoover as: "The Walrasian approach is totalizing. Theory comes first. ⋯ The Marshallian approach is archaeological. We have some clues that a systematic structure lies behind the complexities of economic reality. The problem is how to lay this structure bare. To dig down to find the foundations, modifying and adapting our theoretical understanding as new facts accumulate, becoming ever more confident in our grasp of the super structure, but never quite sure that we have reached the lowest level of the structure. (Hoover, 2006)"

As an illustration, I shall give a brief account of such a Sherlock Holmesian CVAR process and discuss how it has generated new hypotheses that may inspire new economic thinking.

6.1 Puzzling features in the data

Based on standard economic models it is often difficult to explain all the pronounced persistence in economic data, in particular such persistence that seems to originate from other sources than those associated with shocks to technology, preferences and money supply. Also structural breaks are common in economic data but are puzzling viewed from standard RE-based theoretical models. Such breaks can sometimes be handled econometrically by equilibrium mean shifts or changes in mean growth rates but, as Ireland’s RBC model analysis illustrated, can also be of such fundamental character that a split sample analysis is required.

What do we find when analyzing data using the CVAR in the spirit of Sherlock Holmes? A robust finding is that an important regime shift seems to have occurred at the beginning of the eighties. Few models of the macroeconomy are able to pass

\[^{10}\text{This seems similar to the radical fallability idea described in Soros (1998) which indisputably has worked well in the financial sector of the economy. There is no reason why it should not work well in the real economy.}\]
Figure 3: The graphs of relative prices and the nominal exchange rate (mean adjusted) in the upper panel and the real exchange rate lower panel.

statistical tests of parameter constancy over the periods before and after 1980 for the main reason that the division into exogenous and endogenous forces seems to have undergone a change: A new type of persistence influencing the number and the origin of the stochastic trends seems to influence the data after this date.

Why was this? Conventional wisdom would suggest that it was the change in US monetary policy that was the reason for the change. But data consistently refused to tell such a story. However, digging down into the data gave some other clues: the real exchange rates, the real interest rates, and the term spreads were exhibiting a pronounced persistence that seemed untenable with stationarity. The inability to reject the unit root hypothesis suggested that many basic parity conditions, such as the purchasing power parity, the uncovered interest rate parity, the domestic and international Fisher parity, and the Expectations’ hypothesis for the term spread, were not working as standard REH-based theory would predict. As all these variables can be associated with financial market behavior, it seemed plausible that this was related to the world-wide globalization of financial markets. The hypothesis that the ‘new’ puzzling persistence in our macro models is due to speculative behavior in financial markets was generated by Sherlock Holmesian VAR analyses already some twenty years ago.

6.2 Empirical regularities in the financial markets

As the recent and previous financial crises have demonstrated, the booms-and-busts behavior in the stock market and the market for foreign exchange is likely to have a strong impact on the real sector of the economy. Such behavior is hard to explain with REH-based models and has, therefore, often been considered puzzling. In particular, the long swings behavior of real exchange rates under currency floats have
puzzled economists. Figure 3 upper panel illustrates why: the nominal exchange rate moves in long persistent swings around relative prices, which do not exhibit such pronounced swings. The fact that nominal exchange rates exhibit long swings in periods of currency float, whereas relative prices do not, explains why nominal and real exchange rates almost look the same as illustrated in the lower panel of Figure 3.

Such persistent movements away from competitive long-run PPP values are almost bound to have a strong impact on price competitiveness among tradables. In the absence of equilibrium correcting nominal exchange rates, one would, therefore, expect goods prices to equilibrium correct. But, the high variability with which nominal exchange rates move, prevents prices to take the full burden of adjustment. Therefore, to restore equilibrium in the goods market, nominal interest rates would have to compensate for these persistent swings in the real exchange rates, producing a similar persistence in nominal interest rates. The latter is illustrated in the upper panel of Figure 4, which exhibits long and persistent swings in the US-German long-term interest rate differential. Similar persistent swings can be shown for short-term interest rate differentials, albeit with greater variability. Figure 5 demonstrates that the short-long spreads are also highly persistent. Based on a CVAR analysis of five US zero coupon bonds Giese (2008) shows that the term spreads are nonstationary but cointegrated and that shocks to the level and the slope of term structure are pushing the system.

To dig deeper into these data regularities, Johansen and Juselius (1992) and Juselius (1995) first tested a number of joint hypotheses of PPP and UIP based on US-UK data. This was followed up by a similar study of US-Japanese data (Juselius and MacDonald, 2004) and of US-German data (Juselius and MacDonald,
2007). All of them find that the persistent movements in the real exchange rate is compensated by similar persistent movements in the interest rate differential (either short-term or long-term) implying that the long swings movements can be cancelled by cointegration.

How can this be empirically and theoretically understood? Obviously, prices and nominal exchange rates differ in one important respect: nominal exchange rates are primarily being determined in the speculative market for foreign exchange where the trade is based on future expectations, whereas prices of tradables are determined in a very competitive international goods market. This has, of course, also been recognized by many RE-based models such as the Dornbush and Frankel overshooting type of models (Dornbush, 1976 and Dornbush and Frankel, 1995) some of which allow for persistence in the real exchange rate (Benigno, 2004, Engel and West, 1995, Gali and Monacelli, 2005). Nonetheless, Juselius (2009b) shows that the actual swings are too persistent for these models to tell an empirically relevant story. A Sherlock Holmesian CVAR analysis would conclude that the long swings in the real exchange rate remain a puzzle when looked at with REH-based glasses. In contrast, the new IKE-based models proposed by Frydman and Goldberg (2007, 2008) seem to provide a more relevant theoretical framework. In particular, the international monetary IKE based model in Frydman et al. (2008) seems empirically promising.

To test the two competing theories Juselius (2010b) formulated a theory-consistent CVAR scenario for REH-based and IKE-based monetary models. The scenario analysis shows that under RE the real exchange rate and the real interest rate differential are each I(0) or at most near I(1), whereas under IKE they are I(1) or near I(2) and cointegrate to stationarity. One important testable difference is that the degree of persistence is one degree higher under IKE than under REH. Strong evidence for the IKE-based model is found in Frydman et al. (2008), Johansen et al. (2010), Juselius (2010b).

Figure 5: The graphs of the short-long interest spread for USA and Germany.
In the stock market, the efficient market hypothesis is one of the theoretical cornerstones of financial behavior. It has often been formulated as a random walk hypothesis of stock prices, which has been tested (and often not rejected). The random walk hypothesis, however, is much too simplistic as a description of financial market behavior and as a test of the EMH. A more sophisticated formulation was given in the seminal paper by Campbell and Shiller (1987) relying on a REH present value model for stock prices and nominal exchange rates. The model is based on the assumption that both prices and dividends are first difference stationary and that parameters are constant over the full sample period.\footnote{Shiller (2000), in a critique of EMH, concluded that financial markets are essentially driven by irrational exuberance. But under this hypothesis, we would essentially have to give up understanding financial market behavior and how to best cope with them.}

In a still ongoing project, K. Juselius applied the CVAR model to the Shiller data and obtained the following tentative results: (1) a constant equilibrium relationship over the entire sample 1934-2008 is strongly rejected, but reasonably constant sub-samples can be found; (2) first order difference stationarity is rejected in favor of second order difference stationarity; (3) dividends alone cannot explain movements in stock prices, earnings are also needed; (4) stock prices tend to fluctuate in a boom and bust fashion around the price-earnings ratio; (5) earnings are influenced by the price/dividend ratio and are error-correcting toward the price/earnings ratio. Thus, rising earnings lead to rising stock prices, and rising stock prices has a positive “long-run” effect on earnings which, therefore, feed back on stock prices.

These empirical regularities, though still tentative, resembles many of those found in the foreign currency markets and suggests that an IKE based model might work well also in the stock market. For example, under IKE, we would expect that financial behavior is non-constant over time, that endogenously loss averse agents produce near I(2) persistent swings in asset prices, and that this would likely imply strong feed-back effects between prices, dividends and earnings.\footnote{The latter seems consistent with the theory of reflexivity in Soros (1987, 1998, 2001, 2008).} This is what data show.

### 6.3 Implications for macroeconomic modelling

Speculative behavior in the foreign exchange market (through its impact on the real exchange rate, the real interest rate and the term spread) is bound to have strong implication for macroeconomic modelling and policy. This is also the story macroeconomic data tell. The nonstationarity of the term spread and the real interest rate (and indirectly the real exchange rate) is likely to have a strong impact on monetary policy transmission mechanisms. Empirical results in Juselius (1992, 1996, 1998a, 1998b, 1999, 2001, 2004, 2006), Juselius and Toro (2005) and Juselius and Johansen (2006) demonstrate that standard transmission mechanisms for how changes in monetary instruments transmit through the system are seriously impaired by the interference of financial market behavior.

The nonstationarity of the real exchange rate and the real interest rate have been shown to have a strong impact on domestic wage and price setting\footnote{This provides evidence for some important hypotheses in Phelps (1994).} with important implications for fiscal policy. For such empirical evidence see, for example, Juselius
Further evidence supporting the importance of these findings for policy can be found in Bjørnstad and Nymoen (2008), Fanelli (2008) and Juselius, M. (2008) showing essentially no empirical evidence in support of the new Keynesian Phillips Curve model favored by central banks all over the world.

The effect of stock prices on the real economy is also potentially large through their impact on earnings. The latter is likely to have a strong impact on financial and housing wealth and, thus, on consumption and investment behavior. The results in Nyboe-Tabor (2009) suggest that this seems to explain why Ireland’s model variables were not able to explain the data variation over the more recent period.

Thus, the stories data tell when allowed to speak freely seem to broadly reject RE-based models but to be reasonably consistent with an IKE based framework. Data also suggest a strong reflexive relationship between the financial and the real sector of the economy as argued in Soros (1987, 2001, 2008). Thus, by following a Sherlock Holmes type of empirical approach, it seems possible to formulate new hypotheses that should have the potential to inspire new economic thinking.

### 7 Can we trust the stories data tell?

Claiming that one can learn anything from data analysis, is often considered controversial in economics. Many economists would argue that unless the empirical model is constrained by theory from the outset, one would not be able to make sense of the results: Without the mathematical logic of the theory model, one opens up for possibilities of quackery. As some of the CVAR results reported in Juselius and Franchi (2007) were not straightforward to interpret, one might ask, as one of the referee did, whether at the end of the day DSGE modelling with interpretable theory is to be preferred to VAR modelling without theory. No doubt, many economists would be sympathetic to such a view and sometimes for good reasons: There is an abundance of bad VAR applications in the literature. These give the impression of having been applied mechanically (pressing the VAR button) rather than asking sharp and precise questions about the economy. Ireland’s VAR(1) process was just a add-on to the RBC model without any attempt to use it as a source of important information.

Such VAR modeling has nothing to do with a maximum likelihood based VAR analysis. To claim that the statistical analysis is based on full information maximum likelihood requires that the model satisfactorily describes all aspects of the data. This means that the researcher must carefully check for a lot of things: have there been shifts in mean growth rates or in equilibrium means, are the effects of interventions, reforms, and changing policy properly modelled, is the sample period defining a constant parameter regime, is the information set correctly chosen, etc. The accuracy of the results depends on all this being correct in the model. To make the necessary analysis to develop a satisfactory model is a time consuming and tedious process, that depends upon the researcher’s judgement and expertise and has nothing to do with pressing the VAR button. But without such checking, the results can be (and often are) close to useless and if they are taken seriously by policy makers, even worse than worthless.
It is, therefore, important to emphasize that a statistically adequate VAR analysis has to obey equally strict scientific rules as an analysis of a mathematical model in economics. In principle there is no arbitrariness in such empirical analyses as Spanos (2009) points out. However, objectivity can only be achieved provided data are not constrained from the outset in a theoretically prespecified direction because it then would be impossible to know which results are due to the assumptions made and which are the empirical facts. The only way the methodology works properly is by allowing the data to speak as freely as possible about empirical regularities. This is, of course, not the same as letting the data speak without any theory, which generally would not produce anything useful.

Another frequent argument is that the quality of economic data is too low. We agree that economic time series data seldom correspond to the theoretical concepts of a theory model. For example, the representative agent’s income, consumption, and hours worked in Ireland’s model has little in common with the various measurements of aggregate income, private consumption, and total hours worked that he uses in his empirical analysis. While, admittedly, macro data are contaminated with measurement errors, such errors may not be of great concern for the more important long-run analysis, unless they are systematic and cumulate to nonstationarity. Whatever the case, theoretically correct measurements do not exist and, hence, cannot be used by politicians and decision makers to react on. The forecasts, plans and expectations that agents base their decisions on are the observed data and we better understand them, however imperfect they are.

8 Concluding Discussion

The present financial and economic crisis has emphasized the importance of improving our understanding of the reflexive relationship between the financial sector and the real sector of the economy. It has also painfully revealed that extant economic models are seriously lacking in this respect: When the crisis struck policy makers were essentially left to grope in the dark without much guidance for how to ride out the crises. They could only hope that their costly policy measure would have the intended effect (Colander et al. 2009). One reason these models failed to warn economist about the looming crisis was that they are generally based on information rich agents with ‘rational expectations’ and, therefore, assume fast adjustment back towards equilibrium when pushed away. One could say that if the RE hypothesis was a good description of how economic agents behave, data would not have exhibited the persistent behavior away from long-run steady states that preceded the crisis.

Can we do better? In this paper I have argued that one way of improving our models is to learn from the data in a systematic and structured way using available theories and hypotheses, but at the same time to be open to signals in data suggesting that there are other mechanisms we need to understand better. By embedding the theory model in a broader empirical framework, the analysis would be able to point to possible pitfalls in macroeconomic reasoning, and at the same time to generate new hypotheses for how to modify too narrowly specified theoretical models. The clues to the present crisis are hidden in the historical data and we need
to take them much more seriously than usually done to avoid the next one.

The fact that the empirical analysis of Ireland’s model at a first glance seemed impressive, despite its strong empirical rejection when empirically checked, is a warning against drawing conclusions from models based on many untested assumptions. Strong economic priors imposed on the data without testing may say more about the beliefs of the researcher than the state of the economic reality. The ultimate question is, therefore, whether we can afford to let economic policy be guided by beliefs which are not strongly backed up by empirical evidence. If not, I believe extant policy models should be exposed to independent empirical checking and only those who pass should be allowed the label ‘empirically relevant’.

9 References


http://www.nytimes.com/2009/09/06/magazine/06Economic-t.html?_r=4


10 Appendix: Acronyms used in the text

<table>
<thead>
<tr>
<th>Acronym</th>
<th>Term</th>
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<tbody>
<tr>
<td>VAR</td>
<td>Vector Autoregressive</td>
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<tr>
<td>DSGE</td>
<td>Dynamic Stochastic General Equilibrium</td>
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<td>REH</td>
<td>Rational Expectations Hypothesis</td>
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<td>RBC</td>
<td>Real Business Cycle</td>
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<td>TFP</td>
<td>Total Factor Productivity</td>
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<td>CVAR</td>
<td>Cointegrated VAR</td>
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<td>AR</td>
<td>AutoRegressive</td>
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<td>IKE</td>
<td>Imperfect Knowledge Economics</td>
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<tr>
<td>PPP</td>
<td>Purchasing Power Parity</td>
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<tr>
<td>UIP</td>
<td>Uncovered Interest Rate Parity</td>
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